

```

> restart;
x(t) = #prey (rabbits)
y(t) = #predators (wolves)
> de1 := diff( x(t),t ) = alpha1*x(t) - beta1*x(t)*y(t);
      de1 :=  $\frac{d}{dt} x(t) = \alpha_1 x(t) - \beta_1 x(t) y(t)$ 
> de2 := diff( y(t),t ) = +beta2*x(t)*y(t) - alpha2*y(t);
      de2 :=  $\frac{d}{dt} y(t) = \beta_2 x(t) y(t) - \alpha_2 y(t)$ 
> popequil := { rhs( de1)=0, rhs(de2)=0 } ;
      popequil := {  $\alpha_1 x(t) - \beta_1 x(t) y(t) = 0$ ,  $\beta_2 x(t) y(t) - \alpha_2 y(t) = 0$  }
> solve( popequil, {x(t),y(t)} );
      {x(t) = 0, y(t) = 0}, {x(t) =  $\frac{\alpha_2}{\beta_2}$ , y(t) =  $\frac{\alpha_1}{\beta_1}$  }
> alpha1 := 0.1; beta1 := 0.1; beta2 := 0.02; alpha2 := 0.05;
      alpha1 := 0.1
      beta1 := 0.1
      beta2 := 0.02
      alpha2 := 0.05

```

Here's how we get a numerical approximation to the solutions for x(t) and y(t).

```

> F := dsolve( {de1,de2,x(0)=1,y(0)=0.2}, {x(t),y(t)}, numeric );
      F := proc(x_rkf45) ... end proc
> F(0);
      [t = 0., x(t) = 1., y(t) = 0.2000000000000000]
> F(1);
      [t = 1., x(t) = 1.08360311769698, y(t) = 0.194249073977779]
> F(2);
      [t = 2., x(t) = 1.17484203973331, y(t) = 0.188993456628175]

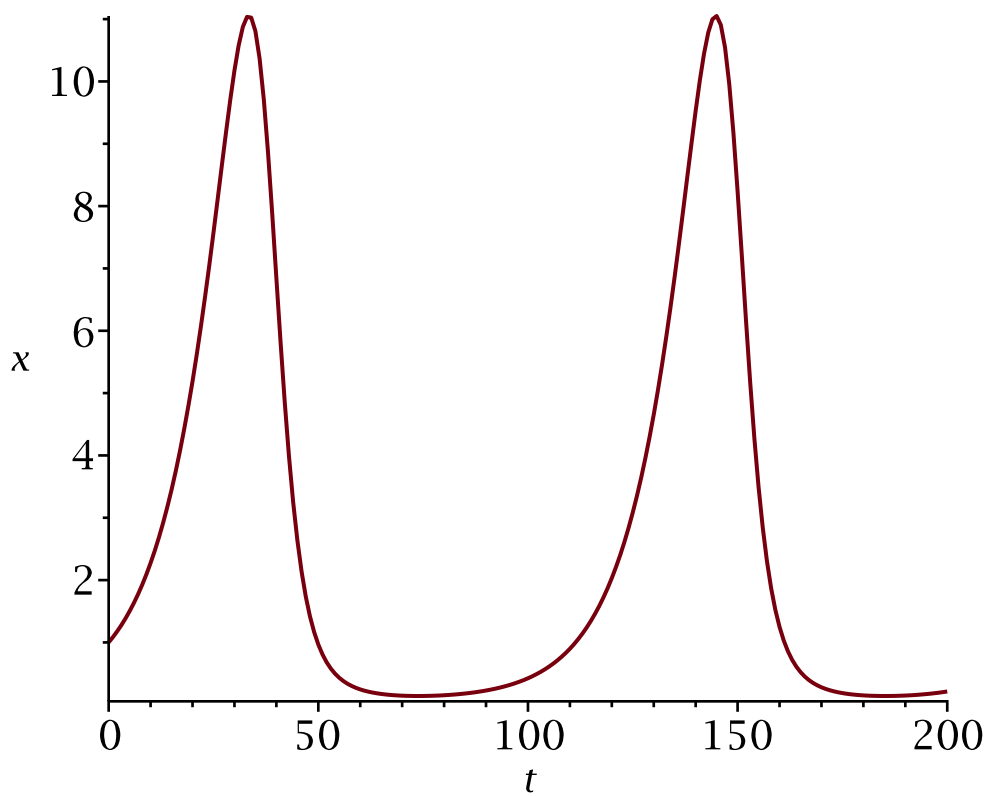
```

To visualize this, the odeplot in the plots package. There are several options.

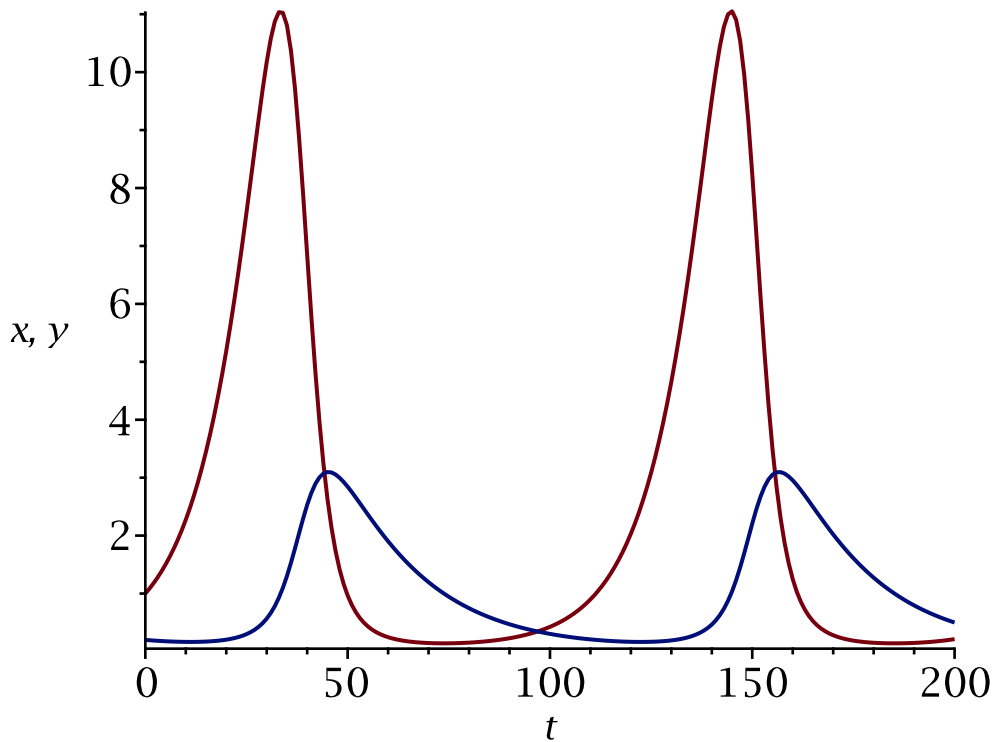
```

> with(plots):
> odeplot( F, [t,x(t)], t=0..200 );

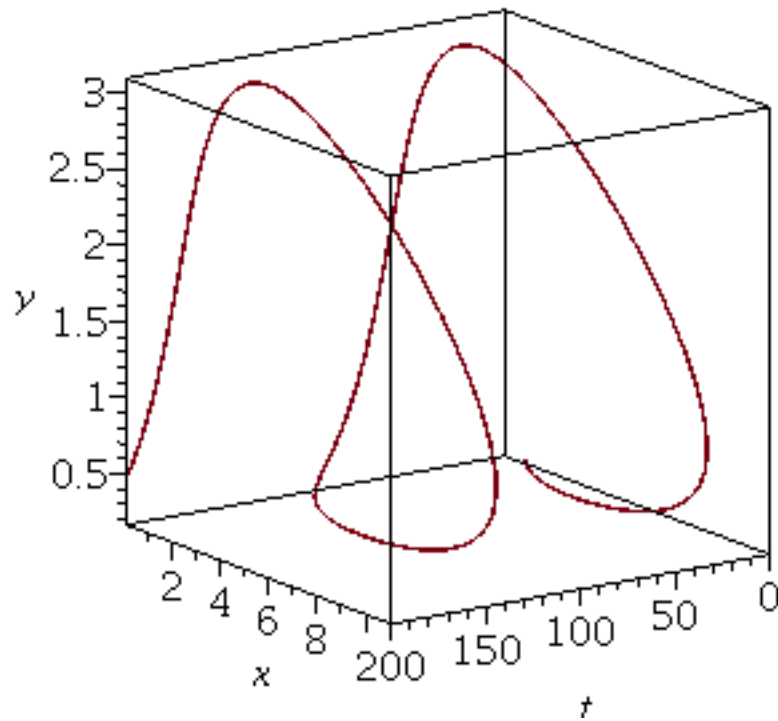
```



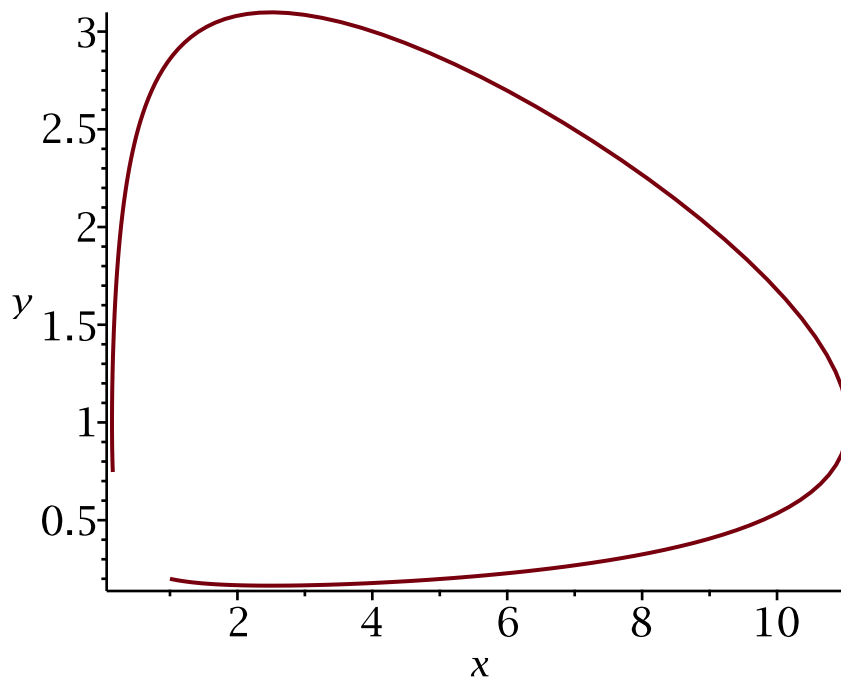
```
> odeplot( F, [[t,x(t)],[t,y(t)]], t=0..200 );
```



```
> odeplot( F, [[t,x(t),y(t)]], t=0..200 );
```



```
> odeplot( F, [[x(t),y(t)]], t=0..80 );
```



The above representation, a plot of  $x$  versus  $y$ , is what DEplot shows.

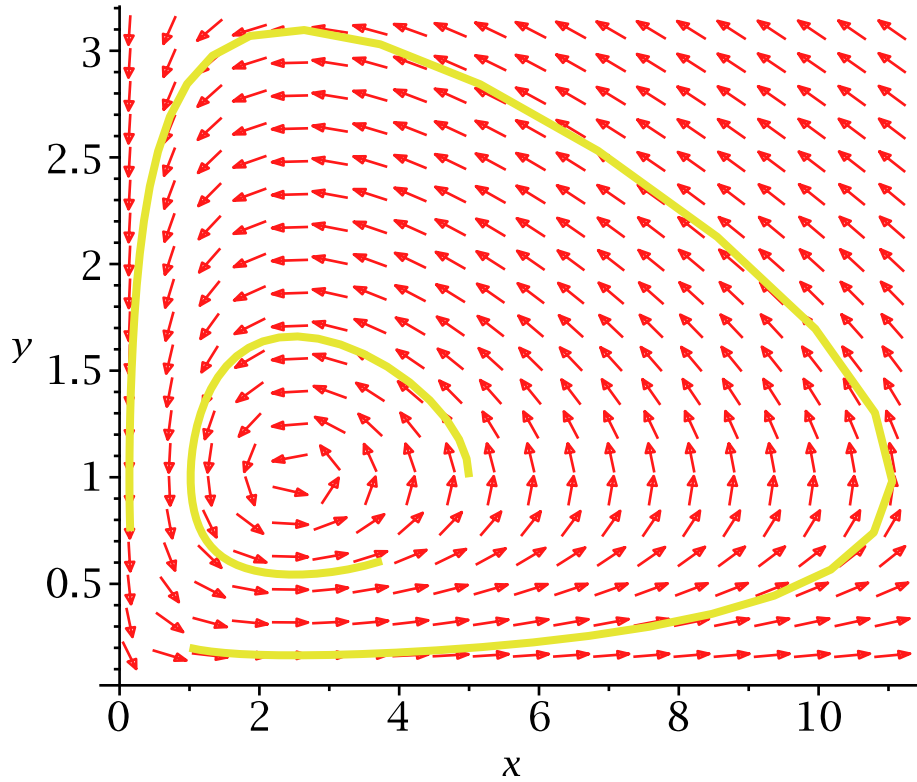
```
> with(DEtools):
```

```
> initvals := [[x(0)=1,y(0)=0.2], [x(0)=5,y(0)=1]];
```

```
initvals := [[x(0) = 1, y(0) = 0.2], [x(0) = 5, y(0) = 1]]
```

```
> DEplot( {de1,de2}, {x(t),y(t)}, t=0..80, initvals, arrows=medium
```

);



The 20 by 20 grid of arrows shows the direction of motion. Random arrow placement is visually much better. A MACM 204 student implemented this.

```
> DEplot( {de1,de2}, {x(t),y(t)}, t=0..80, initvals, arrows=medium,  
numpoints=100,linecolour=blue, dirfield=200 );
```

