MATH 340 Assignment 3, Fall 2017

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This assignment is to be handed in on Wednesday October 11th by 11:20am.
Late penalty: -20% for handing in up to 24 hours late. Zero after that.

Section 1.7: Equations in $\mathbb{Z}_n$

Prove Lemma 1.7.9 part (i).

Section 1.10: Euler's ϕ-function

Exercise 3, 4.

Section 1.11: Theorem's of Euler and Fermat

Exercises 2, 3, 8.

Prove Theorem 1.11.1 (Euler's theorem) using the same approach given in class to prove Theorem 1.11.3 (Fermat's little Theorem). First prove the Lemma: if $a \in \mathbb{Z}_n^*$ then $a\mathbb{Z}_n^* = \mathbb{Z}_n^*$ where $\mathbb{Z}_n^*$ denotes the set of units in $\mathbb{Z}_n$.

Section 2.1: Basic Properties

Exercises 1, 4, 7, 10, 14, 16, 17.
For exercise 10, use the fact that $\mathbb{Q}[\sqrt{2}]$ is a subset of the real numbers $\mathbb{R}$ which is a field, so that you don't have to prove all the field axioms. For exercise 17, give also an example of a zero divisor.

Section 2.2: Subrings and Subfields

Exercises 1, 3(iv), 6, 7, 8, 14, 16.