

```

> restart;
with(LinearAlgebra):
> A,b := RandomMatrix(3,3), RandomVector(3);
      A, b :=  $\begin{bmatrix} 27 & 99 & 92 \\ 8 & 29 & -31 \\ 69 & 44 & 67 \end{bmatrix}, \begin{bmatrix} -32 \\ -74 \\ -4 \end{bmatrix}$ 
> x := LinearSolve(A,b);
      x :=  $\begin{bmatrix} -\frac{54207}{163622} \\ -\frac{207597}{163622} \\ \frac{182389}{163622} \end{bmatrix}$ 
> p := prevprime(10^4);
      p := 9973
Solve  $A \cdot x = b$  modulo  $p, p^2, p^3, \dots$ 
> u := x mod p;
      u :=  $\begin{bmatrix} 4427 \\ 6677 \\ 1922 \end{bmatrix}$ 
> y := iratrecon(u,p);
      y := FAIL
> u := x mod p^2;
      u :=  $\begin{bmatrix} 60351050 \\ 78613863 \\ 95533289 \end{bmatrix}$ 
> y := iratrecon(u,p^2);
      y := FAIL
> u := x mod p^3;
      u :=  $\begin{bmatrix} 432416140013 \\ 251614797504 \\ 410967804788 \end{bmatrix}$ 
> y := iratrecon(u,p^3);

```

$$y := \begin{bmatrix} -\frac{54207}{163622} \\ -\frac{207597}{163622} \\ \frac{182389}{163622} \end{bmatrix}$$

```
> A.y-b;
```

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

```
> d := ilcm( denom(y[1]), denom(y[2]), denom(y[3]) );  
d := 163622
```

```
> A.(d*y)-(d*b);
```

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

```
> ?iratrecon
```